

1. Equivalence between C7 and (LI-7-1 AND LI-7-1 AND LI-7-1 AND LI-7-1)

1.1. When $\mathcal{S}[p][t] = 0$

$C7 = true$, $LI-7-1=LI-7-2= true$

LI-7-3 is satisfied since there is no actual constraint on any $\mathbf{f}[t][p][k][j]$ outside it. Therefore, the equivalence is satisfied

1.2. When $\mathcal{S}[p][t] = 1$

1.2.1. When $\Theta[p][j] \leq 0$, (i.e. $\Theta[p][j] = 0$ since $\Theta[p][j]$ cannot be negative)

$C7 = true$ LI-7-2 is satisfied.

$$\mathcal{S}[p][t] = 1 \Rightarrow \exists k. \mathbf{A}[t][p][k] \geq 1 \Rightarrow \exists k. \mathbf{A}[t][p][k] - \mathcal{S}[p][t] \geq 0 \quad (\text{app.1})$$

$$\Rightarrow \exists k. \mathbf{A}[t][p][k] + \mathbf{f}[t][p][k][j] - \mathcal{S}[p][t] \geq 0 \wedge \mathbf{f}[t][p][k][j] = 0 \quad (\text{app.2})$$

Therefore, LI-7-1 and LI-7-3 are satisfied.

1.2.2. When $\Theta[p][j] > 0$

$C7 \equiv \exists k. \mathbf{A}[t][p][k] > 0 \wedge \mathbf{M}[k][j] \geq \Theta[p][j]$ LI-7-3 imposes that $\exists \mathbf{f}[t][p][k][j] = 0$, therefore LI-7-1 imposes that $\exists \mathbf{A}[t][p][k] \geq \mathcal{S}[p][t]$. i.e. $\exists \mathbf{A}[t][p][k] \geq 1$, i.e. $\exists \mathbf{A}[t][p][k] > 0$

LI-7-2 imposes that for the same t, p, k, j where $\mathbf{f}[t][p][k][j] = 0$, $\mathbf{M}[k][j] - \Theta[p][j] \geq 0$.

Therefore the equivalence is satisfied